

## Fourth Semester B.E. Degree Examination, Dec 08 / Jan 09

## Control Systems

Time: 3 hrs.

Max. Marks:100

Note : 1. Answer any FIVE full questions.

2. Graph papers and semilog graph papers will be supplied.

- a. Define transfer function of a control system. (04 Marks)
- b. For the mechanical system shown in fig.1(b), find the transfer function  $\frac{X_1(s)}{F(s)}$ . (10 Marks)

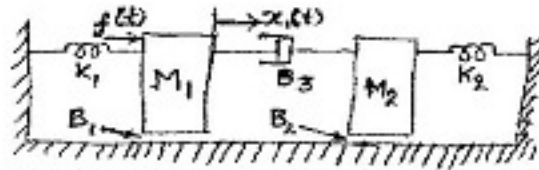


Fig.1(b)

- c. Draw f-v and f-i analogous circuits for fig.1(b). (06 Marks)
- a. State Mason's gain formula. (04 Marks)
- b. For the circuit shown in fig.2(b)  $e_1$  and  $e_2$  are input and output voltages,  $i_1$  and  $i_2$  are loop currents.  $e_1$  is node voltage. Draw a signal flow graph incorporating these variables. (10 Marks)

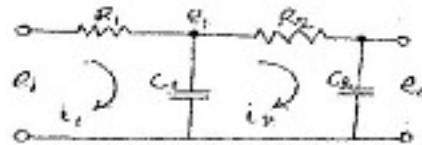


Fig.2(b)

- c. Obtain transfer function  $\frac{E_0(s)}{E_1(s)}$  for the circuit shown in fig.2(b). (06 Marks)
- a. Derive expressions for peak response time  $t_p$  and maximum overshoot  $M_p$  of an under damped second order control system subjected to unit step input. (06 Marks)
- b. Maximum overshoot  $M_p$  and peak time  $t_p$  of an underdamped second order control system subjected to unit step input are respectively 0.163 and 0.363 secs. Find the transfer function of the control system. (07 Marks)
- c. The transfer function of a unity feedback control system is  $G(s) = \frac{K_1}{s(s+2+K_2)}$ . Find the values of  $K_1$  and  $K_2$  so that damping ratio  $\zeta = 0.6$  and the steady state error for ramp input is 0.2 radian. (07 Marks)
- a. What is the effect of feedback on i) the overall gain ii) stability and iii) external disturbance. (08 Marks)
- b. A second order control system is subjected to a unit step input. Sketch the output response curves when damping ratio is i) less than 1, ii) equal to 1 and iii) greater than 1. (04 Marks)
- c. Draw the block diagram of an armature controlled d.c. motor. Obtain transfer function  $\frac{\theta(s)}{E_a(s)}$ , where  $\theta(s)$  is output shaft displacement of motor in radians and  $E_a(s)$  is input armature voltage in volts. (08 Marks)

- 5 a. With zero initial conditions, the system is said to be bounded - input bounded - output (BIBO) stable, or simply stable, if its output  $c(t)$  is bounded to a bounded input  $r(t)$ . Prove the statement. (06 Marks)
- b. Forward path transfer function of a unity feedback control system is  $G(s) = \frac{K}{s(s+10)(s+20)}$ . Determine the range of  $K$  for stability by applying Routh - Hurwitz criterion. Determine the value of  $K$  that will cause sustained constant - amplitude oscillations in the system. Determine the frequency of oscillation. (07 Marks)
- c. The block diagram of a motor control system with tachometer feedback is shown in fig.5(c). Find the range of the tachometer constant  $K$ , so that the system is asymptotically stable. (07 Marks)

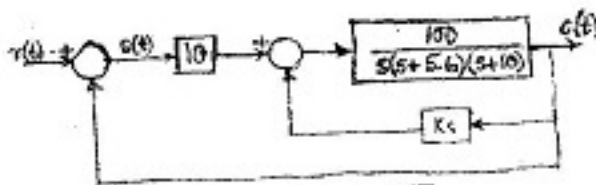


Fig.5(c)

- 6 a. Define the following : i) Relative Stability ii) Absolute Stability iii) Marginal Stability iv) Conditional Stability of a system. (08 Marks)
- b. The open loop T.F of a unity feed back control system is  $G(s) = \frac{K}{s(s+2)(s+4)}$ . Construct the root locus and therefrom, find the value of  $K$  for a damping ratio of 0.5. (12 Marks)
- 7 a. The open loop transfer function of a unity feed back control system is given by  $G(s) = \frac{K}{s(1+0.5s)(1+0.2s)}$ .  
 i) Sketch the Bode magnitude and phase plots for  $k = 10$ . Find phase margin and gain margin. (14 Marks)  
 ii) Determine the value of  $k$ , so that phase margin of the system is  $30^\circ$ . (14 Marks)
- b. Find the transfer function of the system whose Bode magnitude plot is given in fig.7(b). (06 Marks)

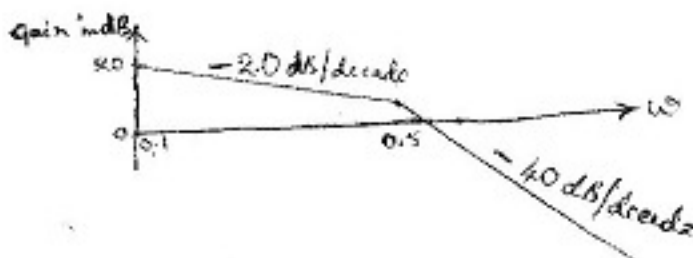


Fig.7(b)

- 8 a. Find the resonant peak, resonant frequency and bandwidth when closed loop transfer function is  $\frac{C(s)}{R(s)} = \frac{5}{s^2 + 2s + 5}$ . (08 Marks)
- b. Discuss the stability of a feedback control system with loop transfer function  $G(s)H(s) = \frac{250}{s(s+5)(s+10)}$ , using the Nyquist stability criterion. (12 Marks)

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